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## Applied Mathematic-II

$2^{\text {nd }}$ Exam/Common/2354/5422/2251/Nov'15

## Duration 3hrs.

## M. Marks 75

## SECTION- A

## Q. 1 (A) Choose the correct answer.

i) Differentiate $\mathrm{x}^{2}$ w.r.t $\mathrm{x}^{3}$ and value is
(a) $\frac{3 x}{2}$
(b) $\frac{2}{3 x}$
(c) $x$
(d) $2 x$
ii) The equation of normal to curve $\mathrm{y}=\sin \mathrm{x}$ at $(0,0)$ is
(a) $\mathrm{X}=0$
(b) $\mathrm{y}=0$
(c) $x+y=0$
(d) $x-y=0$
iii) The probability that a card drawn at random from a pack of cards is a queen is
(a) $\frac{4}{52}$
(b) $\frac{1}{2}$
(c) $\frac{1}{4}$
(d) ) $\frac{1}{13}$
(IV) Which one is a measure of dispersion
(a) Mean
(b) Range
(c) Mode (d) Median
(V) A square Matrix A is singular if $|\mathrm{A}|$ is
(a) 0
(b) 1
(c) 2
(d) 3
B. State True or False
$1 \times 5=5$
i) The square of standard deviation is called variance.
ii) Derivative of $x^{3}$ is $3 x$
iii) $\int e^{x} d x=e^{x}$
iv) $\underset{\theta \rightarrow 0}{L t} \frac{\sin 2 \theta}{2 \theta}=1$
v) The Transpose of a symmetric matrix is equal to itself
(C) Fill in the blanks:
$1 \times 5=5$
i) The probability of tossing a coin of getting a head is $\qquad$ .
ii) $\frac{d(\log x)}{d x}=$
iii) Area of the region bounded by curve $y=x-x^{2}$ between $x=0 \& x=1$ is
IV) Inverse of Matrix A is equal to $\qquad$ -.
V) If $\left|\begin{array}{ll}8 & k \\ 4 & 5\end{array}\right|=0$ then $k=$ $\qquad$ .

## SECTION- B

Q. 2. Attempt any $\frac{\text { Six }}{d x}$ Questions
i) Evaluate $\int \frac{d x}{x^{2}-4 x+8}$
ii) Using trapezoidal rule to find area under the curve whose ordinates are given below

$$
\begin{array}{llccccc}
x & 0 & 1 & 2 & 3 & 4 & 5 \\
y & 0 & 2.5 & 3 & 4.5 & 5 & 7.5
\end{array}
$$

iii) Using Cramer`s rule find the values of $\mathrm{x} \& \mathrm{y}$ from the system of equations:
$2 \mathrm{x}-\mathrm{y}=1$
$7 x-2 y=-7$
IV) A bag contains 6 red, 5 white \& 4 black balls Two balls are drawn, find the probability that none of them is red.
V) Solve differential equation $\frac{d y}{d x}=(4 x+y+1)^{2}$
VI) Evaluate $\int \frac{\sin x}{\sin x-\cos x} d x$
VII) Evaluate $\int_{0}^{\pi / 2} \sin ^{5} x \cos ^{7} x d x$
VIII) If $\mathrm{y}=\mathrm{A} \operatorname{cosn} \mathrm{x}+\mathrm{B} \operatorname{sinn} \mathrm{x}$ show that $\frac{d^{2 y}}{d x^{2}}+n^{2} y=0$
IX) If $x^{y}=y^{x}$ find $\frac{d y}{d x}$

## SECTION- C

## Q. 3. Attempt any Three Questions

$10 \times 3=30$

1) Solve the following equations by matrix method

$$
\begin{aligned}
& 8 x+4 y+3 z=18 \\
& 2 x+y+z=5 \\
& x+2 y+z=5
\end{aligned}
$$

2) Evaluate $\int \frac{x^{2} \boldsymbol{\operatorname { t a n }}^{-1} x}{1+x^{2}} d x$
3) Find standard deviation of the following

| $x$ | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 5 | 10 | 20 | 40 | 30 | 20 | 10 | 4 |

4) Find the maximum \& minimum value of the function $f(x)=x^{4}-6 x^{2}+8 x+11$
5) Differentiate $(\tan x)^{\log x}+x^{x}$ w.r.t. $x$
